

# Input Voltage Range Extension Method for Half-Bridge LLC Converters by Using Magamp Auxiliary Post-Regulator

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## Abstract

An improved half-bridge LLC converter with a magamp auxiliary post-regulator is proposed in this paper. The function of the magamp is bypassed when the converter works within the low input-voltage range. Meanwhile, it operates as an auxiliary post-regulator when the input voltage is high. By changing the blocking time of the magamp, the dc gain of the converter can be extended. Hence, the input voltage range of the converter is extended. The realization of proposed topology does not require a complicated circuit. The controller of the magamp can be easily implemented using only passive components, transistors and an OP amp. The generalized operational principle is analyzed and the design criterion for the magamp is presented. Finally, a 25V output, 400W experimental prototype was built and tested for a 160–300V input-voltage range to verify the feasibility of the proposed method.

**Key words:** LLC converter, Magamp, Post-regulator, Resonance, Wide range

## I. INTRODUCTION

LLC series resonant converters are very popular these days in applications such as adapters, PC power supplies and energy storage systems due to its advantages of high efficiency, high power density and simplicity [1]-[4]. Pulse frequency modulation (PFM) is generally used to control LLC converters. Thus, a wide input-voltage range usually requires a wide switching frequency variation range. However, the slope of the gain curve is extremely flat when the converter operates above the resonant frequency  $f_0$ , i.e., when the input voltage is high, the operating point moves far right away from  $f_0$ . This leads to a significantly increment of the switching loss, and even the output-voltage of the converter may not be regulated to the demanded range. Therefore, a tradeoff between the frequency variation range and the input voltage range are usually made in the conventional LLC

converter design process.

To extend the input-voltage range of an LLC converter, the methods proposed in previous literatures can be cataloged into three groups: 1) precise modeling and parameter optimizing [5]-[7]; 2) multi-stage conversion [8], [9]; 3) topology morphing [10]-[13].

In [5], an accurate LLC converter model is used to estimate the peak gain point, which is useful for wide input-voltage range designs. However, this does not fundamentally change the gain characteristics of an LLC converter. The topology proposed in [8] combines an LLC resonant converter with a boost converter. The LLC converter operates in a relatively narrow frequency range, while the boost converter works with a constant output-voltage. This topology is not conducive to improving the power density of the converter. In [10], the converter works as a full-bridge (FB) LLC converter in the low input-voltage range. Meanwhile, for the high input voltage range, it is changed to a half-bridge (HB) LLC converter. However, its output exhibits severe overshoots/undershoots at the topology transition instants. The control method proposed in [11] improved the idea in [10] by maintaining a tight regulation of the output during transitions. However, it

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is not suitable for applications that require a fast feedback response due to its long transition period. The topology reported in [12] employed a bidirectional switch which can halve the input-voltage of the resonant tank when a low voltage gain is needed. However, there are six MOSFETs which increase the complexity and the cost of the circuit. The topology proposed in [13], integrates two half-bridges in series to construct a three-level LLC converter, which can double the input voltage range. However, a potential voltage unbalance on the input capacitors may occur due to the mismatch of the switching periods and/or transformer windings. Furthermore, there is no simple method specifically for HB LLC converters in the literatures.

In order to overcome the problems mentioned above, an input voltage range extension method for HB LLC converters is proposed in this paper using magamp auxiliary post-regulators. The magamp has been well investigated for use in multiple output converters, including LLC converters [14]. In multiple output applications, magamp is used to distribute the conduction time for different outputs. The energy transmission between the primary side and the secondary side is not completely blocked. Unlike [14], for the proposed single output LLC converter, the magamp is used to completely cut off the energy exchange between the primary and secondary sides to change the dc gain curve of the converter. In the low input voltage range, the converter works as a conventional HB LLC converter. In the high input voltage range, the output voltage of the converter can be regulated by changing the blocking time of the magamp with a fixed switching frequency.

This paper is organized as follows. Section II analyzes the operating principle of the proposed converter in detail. Section III presents the characteristics and design consideration of the proposed converter. In section IV, an experimental prototype is built and tested to verify the theoretical analysis. Finally, section V gives the conclusion.

## II. PROPOSED HB LLC CONVERTER WITH AUXILIARY MAGAMP POST-REGULATOR

### A. Limitations of an LLC Converter in Wide Input-Voltage Range Applications

Traditional HB LLC converters usually change the switching frequency to regulate the output against input voltage changes. Frequency control is achieved by operating the switches with a constant duty cycle of approximately 0.5. A proper switching dead-time between the two switches is provided to achieve zero voltage switching (ZVS) [15]. The dc gain curve of an HB LLC converter according to fundamental harmonic approximation (FHA) is shown in Fig. 1. The converter is designed to work in the inductive region where the ZVS of the primary switches can be achieved over the entire input voltage condition. Since the input voltage of the converter is changed

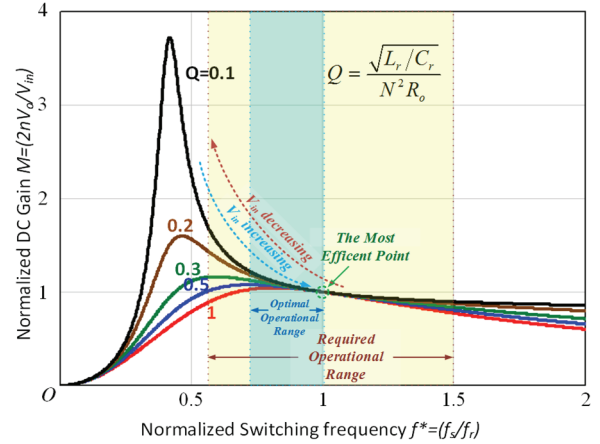


Fig. 1. DC Gain curve of a conventional HB LLC converter.

and the output current of the converter varies, the dc voltage gain value of the converter is changed. In order to meet the varied gain value, a conventional LLC converter can operate below or above the resonant frequency. As can be seen in Fig. 1, the dc gain increases as the frequency increases and the  $Q$  factor decreases, while the dc gain decreases when the frequency increases. The most efficient point occurs around the resonant frequency  $f_0$ . When the switching frequency  $f_s$  is lower than  $f_0$ , the lower  $f_s$  is, the larger the circulating current is. On the other hand, the switching losses increases as the frequency increases. When the switching frequency is above  $f_0$ , the rectification diodes  $D_1$  and  $D_2$  at the secondary side lose the ZCS condition. To meet an optimal frequency, the LLC converter should be operated under a very small frequency range around  $f_0$ , as illustrated in Fig. 1. On the other hand, a wide input voltage or load-current range requires a wide switching frequency range. In order to reduce the switching frequency variation range, a low  $K$  (denoted by  $h$  in some studies) [16], i.e., the inductor ratio ( $L_m/L_r$ ), is typically used in the LLC converter design. However, the inductor  $L_m$  decreases as  $K$  becomes lower. Since a small  $L_m$  means an increase in the conduction loss, it is not beneficial to improve the efficiency of the converter.

### B. Proposed Topology Description

The proposed HB LLC converter with magamp auxiliary post-regulator (LLC-MAP) is illustrated in Fig. 2(a). When compared with the conventional HB LLC converter, the proposed topology adds two magamps ( $S_{r1}$  and  $S_{r2}$ ) in serial with the rectification diodes  $D_1$  and  $D_2$  respectively on the secondary side. Moreover, a switch  $S_W$  and a frequency limiter are added to the feedback loop. The “on/off” status of  $S_W$  is determined by the switching frequency  $f_s$  and the upper frequency limit  $f_{max}$ . In practice,  $f_{max}$  is set slightly smaller than  $f_0$  to insure ZCS of  $D_1$  and  $D_2$ . In the low input-voltage range,  $f_s$  is lower than  $f_0$  and  $S_W$  is gated off.  $V_o$  is regulated by changing  $f_s$  the same as the conventional HB LLC converter. This state is called the variable-frequency mode (VF Mode). When the

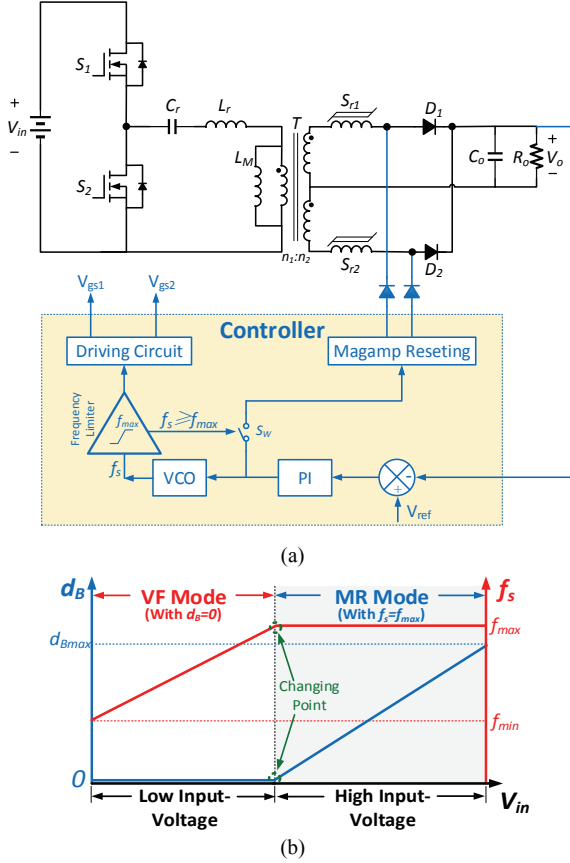


Fig. 2. Proposed topology: (a) LLC resonant converter with magamp post-regulator; (b) Conceptual control diagram of an LLC-MAP converter.

input-voltage increases,  $f_s$  moves up accordingly to reduce the dc gain of the converter. Once  $f_s$  meets the upper limit  $f_{max}$ ,  $f_s$  is restricted to the constant value  $f_{max}$  and  $S_W$  turns on. Then  $V_o$  is regulated by the magamp regulator loop at a fixed-frequency as shown in Fig. 2(b). This state is called the magamp-regulation mode (MR Mode).

### C. Operational Principle

As mentioned previously, the proposed LLC-MAP converter has different operational principle during different modes. In the VF mode, the magamps are equivalent to copper wires with very small impedances. The LLC-MAP converter has the same structure as a conventional HB LLC converter. The operational principle is also the same as that of a conventional HB LLC converter.

In the MR mode, as shown in the operational waveforms in Fig. 3, one switching cycle can be divided into eight stages. Equivalent circuits of the stages 1-4 are shown in Fig. 4. For convenience, the following assumptions should be made.

- 1) The output capacitor  $C_o$  is large enough to neglect the voltage ripple on  $V_o$ . Thus,  $V_o$  is assumed to be constant.
- 2) The parasitic capacitors of the primary switches and the junction capacitors of the secondary diodes are not shown in the circuit for the sake of simplicity.

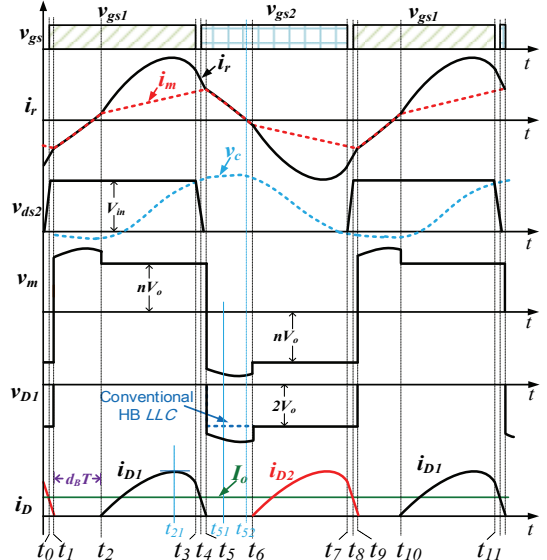


Fig. 3. Principle waveforms of an LLC-MAP converter in the MR mode.

**Stage 1** [ $t_0$ - $t_1$ ] [see Fig. 4(a)]: Before  $t_0$ , the body diode of  $S_1$  has conducted. The differential current between  $i_m$  and  $i_r$  feeds the load through  $D_2$ . At  $t=t_0$ ,  $S_1$  turns on under the ZVS condition. Due to forward biasing of  $D_2$ , the voltage across  $L_m$  is clamped by  $(-nV_o)$ . Resonance occurs between  $L_r$  and  $C_r$ . The resonance frequency is  $f_0 = 1/(2\pi\sqrt{L_r C_r})$ . When  $i_m$  is equal to  $i_r$  at  $t_1$ ,  $D_2$  turns off under the ZCS condition.

**Stage 2** [ $t_1$ - $t_2$ ] [see Fig. 4(b)]:  $S_{r1}$  was reset in the previous switching cycle. At  $t=t_1$ , a voltage  $(v_{Tsec}-V_o)$  appears across  $S_{r1}$  and  $D_1$  in series. This is in the direction to drive the magamp core up towards the saturated state. There are only very small coercive current flows through  $S_{r1}$ . Thus,  $S_{r1}$  is equivalent to an “opened” switch. In the meantime,  $S_{r2}$  is reset by the voltage  $v_{Tsec}$ . On the primary side, resonance occurs between  $C_r$  and  $(L_m+L_r)$ . The resonance frequency is  $f_m = 1/[2\pi\sqrt{(L_r+L_m)C_r}]$ . This stage ends when  $S_{r1}$  is saturated at  $t_2$ .

In this stage, the resonant current only circulates through the resonant tank and  $S_1$ , and there is almost no power transferred to the secondary side. Thus, this stage is named the blocking interval. The blocking time can be expressed as the following expression according to Faraday’s Law:

$$t_B = t_2 - t_1 = \frac{n_{Sr} \Delta B A_e}{V_{Tsec}^B - V_o} \quad (1)$$

where  $n_{Sr}$  is the turn number of the magamp,  $A_e$  is the effective core area of the magamp core,  $\Delta B$  is the magnetic induction intensity increment from the initial state to the saturated state, and  $V_{Tsec}^B$  is the average voltage of  $v_{Tsec}$  during the blocking interval. The blocking duty ratio is  $d_B = 2t_B/T$ .

**Stage 3** [ $t_2$ - $t_3$ ] [see Fig. 4(c)]: At  $t_2$ ,  $S_{r1}$  has been magnetized to the saturated state, and is equivalent to a “closed” switch.  $D_1$

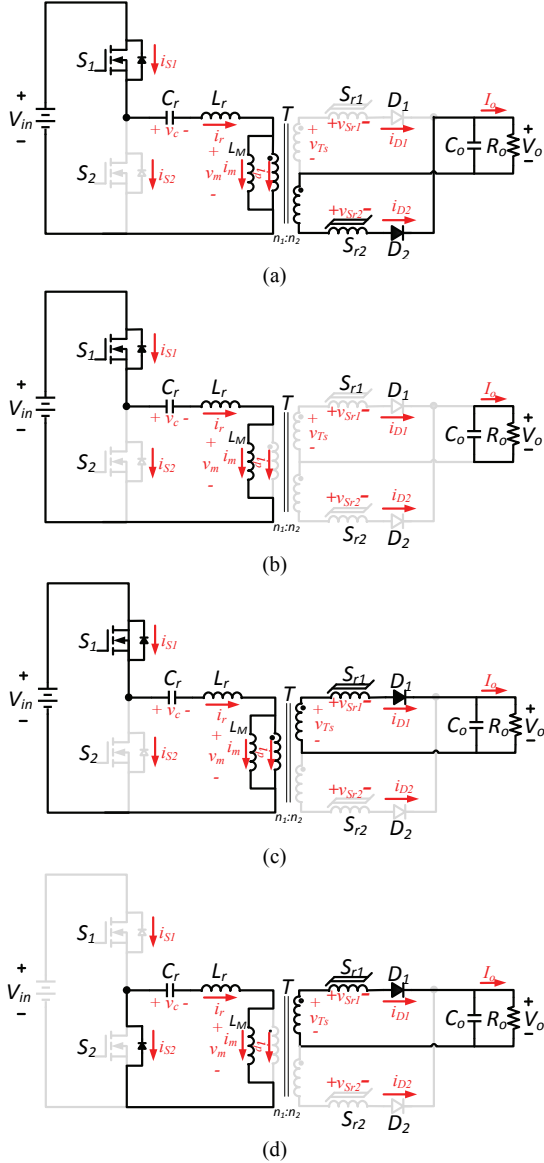


Fig. 4. Equivalent circuits of the proposed LLC-MAP converter: (a)  $[t_0-t_1]$ ; (b)  $[t_1-t_2]$ ; (c)  $[t_2-t_3]$ ; (d)  $[t_3-t_4]$ .

is forward biased and the primary side of the transformer is clamped by  $nV_o$ . Resonance occurs between  $L_r$  and  $C_r$ . The current  $i_r$  increases rapidly with a sinusoidal wave type, while  $i_m$  increases linearly. The deference between  $i_r$  and  $i_m$  is transferred to the secondary side. This stage is terminated at  $t_2$  when  $i_r=i_m$ .

**Stage 4**  $[t_3-t_4]$  [see Fig. 4(d)]: At  $t_3$ ,  $S_1$  is turned off. The parasitic capacitance of  $S_1$  is charged by the resonant current and the drain-source voltage of  $S_1$  increases. In the meantime, the parasitic capacitance of  $S_2$  is discharged until its body-diode conducts. Then the ZVS turning on condition for  $S_2$  can be achieved.

Due to symmetry, the operation stages 5-8 are the same as 1-4 except that the resonance is initiated by the storage energy in the resonant capacitor  $C_r$ .

### III. CHARACTERISTICS AND DESIGN CONSIDERATIONS

#### A. DC Voltage Gain

In this paper, the normalized input-to-output dc voltage gain of the LLC-MAP converter is defined as:

$$M = \frac{2nV_o}{V_{in}} \quad (2)$$

Since the proposed HB LLC converter should operate below or close to the limit frequency  $f_{max}$  in the VF mode, as shown in Fig. 2, the FHA approach can be used for the dc gain analysis of the converter. This means that only the fundamental component of the input square wave is effective for transferring energy to the output. At this state, the dc voltage gain of the LLC-MAP is the same as that of a conventional HB LLC converter as shown in Fig. 5(a).

When the LLC-MAP converter works in the MR mode, the switching frequency is fixed at  $f_s = f_{max} \cong f_0$ . It is obvious that  $M=1$  if  $d_B=0$ , and that  $M=0$  if  $d_B=1$ . Therefore, it is easy to understand that the output voltage is proportional to  $d_B$ , and that the voltage gain can be continuously regulated to between 1 and 0 by varying  $d_B$  between 0 and 1. Next, an accurate derivation of the dc gain is made for the MR mode. Because there are more high-order harmonics that cannot be neglected when the LLC-MAP converter works in the MR mode, the FHA method is not accurate enough. Hence, the steady-state method is employed in the following derivation process. In order to simplify the analysis in this section, normalized variables are used in the following expressions. Define the voltage, current, and frequency bases as:

$$\begin{cases} V_{BASE} = nV_o \\ I_{BASE} = nV_o / Z_r \\ f_{BASE} = f_r \end{cases} \quad (3)$$

where the characteristic impedance of the converter is  $Z_r = \sqrt{L_r / C_r}$ . In the following description,  $x^*$  is the normalized value of  $x$ , i.e.,  $x^* = x / X_{BASE}$ . Therefore,  $i_r^*$ ,  $i_m^*$  and  $v_c^*$  are the normalized values of the inductor current  $i_r$ ,  $i_m$  and the capacitor voltage  $v_c$ .

In stage 1, the expressions of  $i_r$ ,  $i_m$  and  $v_c$  can be normalized as:

$$\begin{cases} i_{r1}^*(\theta) = I_{r1}^* \sin(\theta + \theta_{10}) \\ i_{m1}^*(\theta) = I_{m1}^* - \frac{\theta}{m-1} \\ v_{c1}^*(\theta) = \frac{1}{M} + 1 - I_{r1}^* \cos(\theta + \theta_{10}) \end{cases} \quad (4)$$

Where  $\theta = 2\pi f_0 t$ ,  $m = (L_m + L_r) / L_r$  and  $\theta_{10}$  is the initial phase angle in stage 1.  $I_{r1}$  and  $I_{m1}$  are the initial values of  $i_r$  and  $i_m$  in stage 1.

In stage 2, the expressions of  $i_r$ ,  $i_m$  and  $v_C$  can be normalized as:

$$\begin{cases} i_{r2}^*(\theta) = i_{m2}^*(\theta) = I_{r2}^* \sin\left(\frac{\theta}{\sqrt{m}} + \theta_{20}\right) \\ v_{C2}^*(\theta) = \frac{1}{M} - \sqrt{m} I_{r2}^* \cos\left(\frac{\theta}{\sqrt{m}} + \theta_{20}\right) \\ v_{m2}^*(\theta) = \frac{(m-1)I_{r2}^*}{\sqrt{m}} \cos\left(\frac{\theta}{\sqrt{m}} + \theta_{20}\right) \end{cases} \quad (5)$$

where  $\theta_{20}$  is the initial phase angle in stage 2.  $I_{r2}$  is the initial value of  $i_r$  and  $i_m$  in stage 2.

In stage 3, the expression of  $i_r$ ,  $i_m$  and  $v_C$  can be normalized as:

$$\begin{cases} i_{r3}^*(\theta) = I_{r3}^* \sin(\theta + \theta_{30}) \\ i_{m3}^*(\theta) = I_{m3}^* + \frac{\theta}{m-1} \\ v_{C3}^*(\theta) = \frac{1}{M} - 1 - I_{r3}^* \cos(\theta + \theta_{30}) \end{cases} \quad (6)$$

where  $\theta_{30}$  is the initial phase angle in stage 3.  $I_{r3}$  and  $I_{m3}$  are the initial values of  $i_r$  and  $i_m$  in stage 3.

For the sake of simplicity, stage 4, which is short enough, is neglected in the dc gain analysis. Each of the operating phases is limited by the boundary conditions at the connection and switching moments of their adjacent phases. The current flows through the inductor and the voltage across the capacitor should maintain continuity between the two stages. Thus, the continuity conditions can be expressed as:

$$\begin{cases} i_{r1}^*(\theta_1) = i_{r2}^*(0) \\ i_{m1}^*(\theta_1) = i_{m2}^*(0) \\ v_{C1}^*(\theta_1) = v_{C2}^*(0) \\ i_{r2}^*(\theta_2) = i_{r3}^*(0) \\ i_{m2}^*(\theta_2) = i_{m3}^*(0) \\ v_{C2}^*(\theta_2) = v_{C3}^*(0) \end{cases} \quad (7)$$

For periodic operation, the ending values of  $i_r$  and  $i_m$  in stage 3 should be opposite their initial values in stage 1 due to symmetry in a half cycle, as shown in Fig. 3. Thus, the symmetry conditions are given by:

$$\begin{cases} i_{r3}^*(\theta_3) = -i_{r1}^*(0) \\ i_{m3}^*(\theta_3) = -i_{m1}^*(0) \end{cases} \quad (8)$$

Because there is a  $V_{in}/2$  dc voltage bias on  $C_r$  for half-bridge converters, the symmetry condition of  $v_C$  is:

$$v_{C3}^*(\theta_3) = \frac{1}{M} - v_{C1}^*(0) \quad (9)$$

Only stage 1 and stage 3 are involved in the power delivery between the primary side and the secondary side in a half cycle. Thus, the normalized output power can be expressed as:

$$p_o^* = \frac{f_s^*}{\pi} \left[ \int_0^{\theta_1} (i_{m1}^* - i_{r1}^*) d\theta + \int_0^{\theta_3} (i_{r3}^* - i_{m3}^*) d\theta \right] \quad (10)$$

The output power can also be expressed as:

$$p_o^* = V_o^* I_o^* = \frac{8Q}{\pi^2} \quad (11)$$

Substituting (11) into (10) yields:

$$\frac{8Q}{\pi} = \int_0^{\theta_1} (i_{m1}^* - i_{r1}^*) d\theta + \int_0^{\theta_3} (i_{r3}^* - i_{m3}^*) d\theta \quad (12)$$

Note that  $\theta_1 + \theta_2 + \theta_3 = \pi / f_s^*$ . Therefore, it is possible to obtain:

$$d_B = 1 - (\theta_1 + \theta_3) / \pi \quad (13)$$

By combining (4)-(9), (12) and (13) after a proper manipulation, the following simplified constrain equations can be derived:

$$\begin{cases} I_{r1}^* \sin(\theta_1 + \theta_{10}) - I_{r2}^* \sin(\theta_{20}) = 0 \\ 1 + \sqrt{m} I_{r2}^* \cos(\theta_{20}) - I_{r1}^* \cos(\theta_1 + \theta_{10}) = 0 \\ I_{r2}^* \sin(\theta_2 / \sqrt{m} + \theta_{20}) - I_{r3}^* \sin(\theta_{30}) = 0 \\ 1 - \sqrt{m} I_{r2}^* \cos(\theta_2 / \sqrt{m} + \theta_{20}) + I_{r3}^* \cos(\theta_{30}) = 0 \\ I_{r3}^* \sin(\theta_3 + \theta_{30}) + I_{r1}^* \sin(\theta_{10}) = 0 \\ I_{r2}^* \sin(\theta_2 / \sqrt{m} + \theta_{20}) + I_{r2}^* \sin(\theta_{20}) + (\theta_1 + \theta_2) / m - 1 = 0 \\ 1/M - I_{r3}^* \cos(\theta_3 + \theta_{30}) - I_{r1}^* \cos(\theta_{10}) = 0 \\ I_{r2}^* [\cos(\theta_{20}) - \cos(\theta_2 + \theta_{20}) - \theta_2^2 / (2m-2) - 8Q/\pi] = 0 \\ 1 - d_B - (\theta_1 + \theta_3) / \pi = 0 \end{cases} \quad (14)$$

There are ten unknown variables ( $I_{r1}^*$ ,  $I_{r2}^*$ ,  $I_{r3}^*$ ,  $\theta_1$ ,  $\theta_3$ ,  $\theta_{10}$ ,  $\theta_{20}$ ,  $\theta_{30}$ ,  $M$  and  $d_B$ ) in the above function. Since (14) is a transcendental function, the results of  $M$  versus  $d_B$  cannot be directly obtained. When  $m=7$  and  $f_s^*=1$ , by numerically solving the distribution equation (14) with the *fsolve(x)* function in MATLAB, the characteristics of  $M$  versus  $d_B$  can be depicted for different values of  $Q$  as shown in Fig. 5(a). As can be seen, when  $d_B$  is zero, the converter works as a traditional HB LLC converter if the initial blocking time of the magamp is neglected. When  $d_B$  is 1, there is no energy transferred to the load when the transformer works in the open state. The quality factor  $Q$  has a slight effect on the dc gain, and the dc gain is mainly determined by  $d_B$ .

A comparison between the LLC-MAP converter in the MR mode and the conventional LLC converter is illustrated in Fig. 5(b). As can be seen, a much higher frequency is needed in the conventional LLC converter when the same dc gain is required. In addition, it is not sensitive to  $Q$ , the output load in other words, when the LLC-MAP converter works in the MR mode.

### B. Design of the Magamp Auxiliary Post-Regulator

As shown in Fig. 6(a), a current reset circuit can be adopted for the magamp due to a reduced phase delay and no need for negative voltage power [17]. The blocking time of the magamp is regulated by means of its resetting current  $I_{rst}$ , which is proportional to the error voltage  $v_{EA}$ . As can be seen



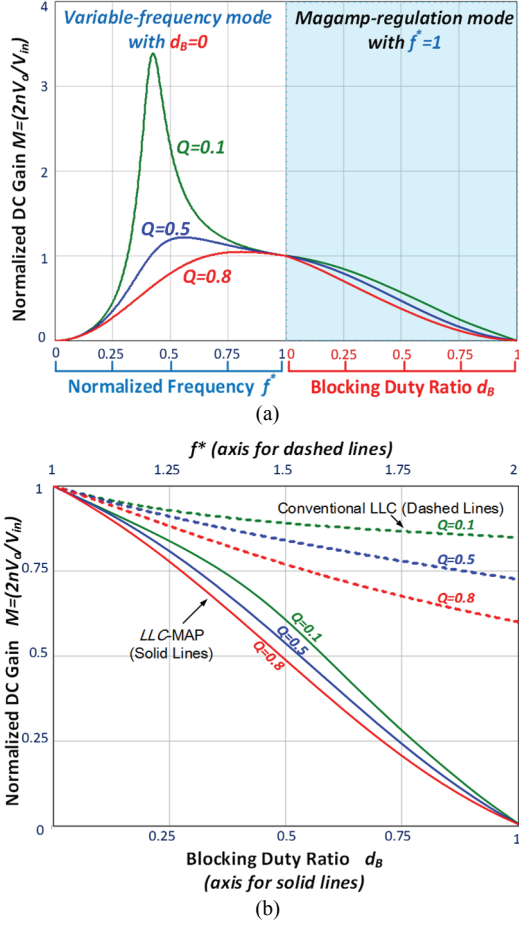


Fig. 5. Voltage gain curves of: (a) Proposed LLC-MAP converter; (b) Comparison between the LLC-MAP converter and the conventional HB LLC converter.

in Fig. 6(b), during  $[t_5-t_{51}]$ , the magamp current  $i_r$  decreases from zero to  $I_{rst}$  almost linearly. The diode  $D_{r1}$  conducts. Therefore,  $v_{Sr}=V_{Tsec}$ . When  $i_r$  reaches  $I_{rst}$  at  $t=t_{51}$ ,  $v_{Sr}$  decrease to zero exponentially. The decreasing transient interval is relatively short and can be neglected. The magamp inductor reset is finished at  $t=t_{51}$ . The relationship between unsaturated inductance of the magamp  $L_{Sr}^{unsat}$  and  $I_{rst}$  is:

$$L_{Sr}^{unsat} = \frac{V_{Tsec}^{rst} t_{rst}}{I_{rst}} \quad (15)$$

where,  $V_{Tsec}^{rst}$  is the average voltage of  $v_{Tsec}$  during the resetting interval. The volt-second balance during the blocking and resetting intervals yields:

$$(V_{Tsec}^B - V_o) \cdot t_B = V_{Tsec}^{rst} t_{rst} \quad (16)$$

i.e.,  $\Lambda_1 = \Lambda_2$  in Fig. 6(b). It should be noted that, at the blocking interval,  $v_{Sr}=V_{Tsec}-V_o$  should be positive to ensure that the magamp core can reach saturation. The maximum  $t_B$  can be achieved when  $v_{Sr}=0$ . A proper magamp core can be selected according to its maximum blocking time and unsaturated inductance.

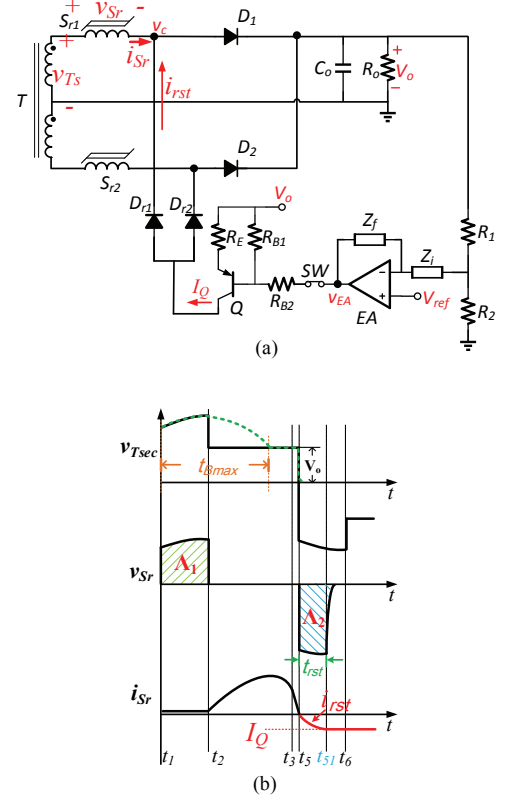


Fig. 6. Operating principle of the magamp: (a) Resetting circuit of the magamp; (b) Key waveforms for the magamp regulator.

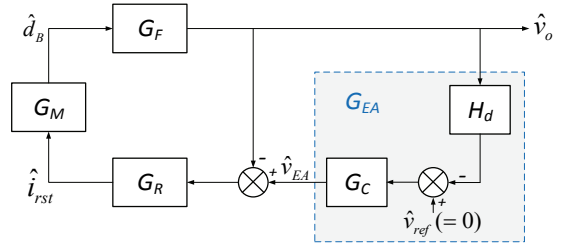


Fig. 7. Control block diagram of the magamp post-regulator in the LLC-MAP converter.

### C. Design of the Feedback Controller

Small signal control block diagrams for the magamp post-regulator in the LLC-MAP converter are illustrated in Fig. 7, where the  $\hat{\cdot}$  sign denotes the small-signal ac quantity,  $G_R$  presents the reset circuit transfer function,  $G_M$  presents the magnetic modulator transfer function, and  $G_F$  presents the duty cycle to output the voltage transfer function.

According to the specific circuit in Fig. 6(a), by equating the ac perturbation quantities in the small-signal model, the gain of each of the blocks can be exacted as:

$$G_R = \frac{\hat{i}_{rst}}{\hat{v}_o - \hat{v}_{EA}} = \frac{-R_{B1}}{(R_{B1} + R_{B2})R_E} \quad (17)$$

$$G_M = \frac{\hat{d}_B}{\hat{i}_{rst}} = \frac{L_{Sr}^{unsat} f_s}{V_{Ts} - V_o} \quad (18)$$

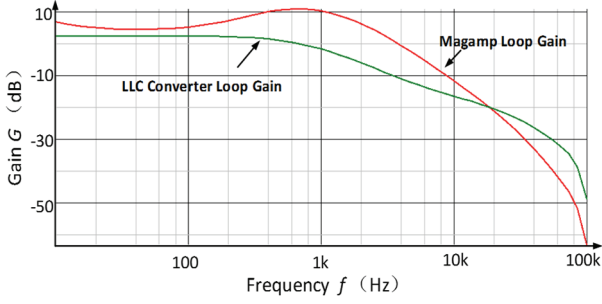


Fig. 8. Comparison of the open loop gain curves between the magamp loop and the LLC loop.

$$G_F = \frac{\hat{v}_o}{\hat{d}_B} = \frac{sR_o V_{Ts}}{s^2 R_o L_{sr}^{sat} C_o + sL_{sr}^{sat} + R_o} \quad (19)$$

where,  $L_{sr}^{sat}$  is the inductance of the saturated magamp. The open loop transfer function of the magamp post-regulator can be expressed as:

$$G_{VC\_MAG} = \frac{\hat{v}_o}{\hat{v}_{EA}} = \frac{G_R G_M G_F}{1 + G_R G_M G_F} \quad (20)$$

Given specific parameters, as shown in Fig. 8, a comparison of the open loop gain curves between the magamp loop and the LLC loop can be obtained by a mathematic tool. As can be seen, the two loops exhibit strong intersections. In other words, the magamp post-regulator can share a controller with the LLC loop. In practice, the compensator parameters need to be selected based on the worst case of the bandwidth.

#### D. Loss Analysis of the Magamp

As mentioned previously, the output diode turns off under the ZVS condition. The dead-time problem of the magamp is neglectable in the LLC converter [14]. In the VF mode, the reset current is zero and the magamp is equivalent to a short circuit. There is only the copper loss introduced into the converter. The power dissipated in the magamps can then be written as:

$$P_{Mag}^{Cu} = \frac{I_o^2 \rho n_{sr} M_{LT}}{A_w} \quad (21)$$

where  $\rho$  is the wire resistivity,  $M_{LT}$  is the mean length per turn of the winding, and  $A_w$  is the size of the wire. Since the winding of the magamp is only a few turns, in the total loss, the copper loss accounts for no more than 0.3% in the experimental prototype.

In the MR mode, the core loss of the magamp should also be considered. It can be expressed as:

$$P_{Mag}^{Core} = 2\Delta B H_R A_C l_m f_s \quad (22)$$

where  $\Delta B = (V_{Tsec}^B - V_0) \cdot t_B$ ,  $H_R$  is the coercive force needed for the reset,  $A_C$  is the core cross-sectional area, and  $l_m$  is the length of the magnetic path. The core loss data in W/kg as a

function of the flux density and the frequency can also be found in datasheets in the form of a table or an equation. After giving the specific parameters of the prototype, the loss reaches the maximum proportion, which is about 0.9% at the maximum blocking time.

In the VF mode, the LLC-MAP converter fully inherits the high efficiency advantages of the conventional LLC converter. In the MR mode, despite the conversion efficiency decreases caused by the magamp core loss, a wide input-voltage range can be achieved without varying the switching frequency in a wide range, which reduces the switching losses. Therefore, the efficiency impact of the two magamps is affordable.

In summary, when the input-voltage is within the working range of the traditional LLC, the conversion efficiency of the LLC-MAP is basically the same. When the input voltage is out of the working range of the traditional LLC, the LLC-MAP converter makes a tradeoff for a wider input-voltage range with acceptable losses increase.

#### E. Performance Comparison

The proposed method gives a hint that the input-voltage range of an LLC converter may also be regulated through the secondary-side post-regulator. Although adding two magamps leads to additional cost, the proposed converter uses two MOSFETs less than the primary-side variable-structure LLC converters presented in [13]-[15]. The price of a magamp in this application is roughly equal to the price of a MOSFET. However, the proposed control circuit only adds several diodes, transistors and resistors to the control circuit, while a more expensive digital processor and isolated MOSFET drivers should be employed in a primary-side variable-structure. Therefore, considering the entire system, the proposed method has a price advantage.

On the other hand, primary-side variable-structures usually suffer from overshoot/undershoot problems on the output during mode transitions. In general, to overcome these problems, some complex algorithms have been applied. In the LLC-MAP converter, the LLC loop and the magamp loop have essentially the same frequency-response characteristics. Both of them can share a feedback controller, which is very simple. This gives the converter the advantage of a fast response. Therefore, during mode transitions, the output voltage can be smoothly regulated.

It should be noted that each of the solutions has advantages and disadvantages. The structure proposed is a good candidate for a wide input analog-controlled LLC converter. The LLC-MAP converter can be combined with a primary-side variable-structure to further extend the operational range in a future work.

## IV. EXPERIMENTAL PERFORMANCE EVALUATION

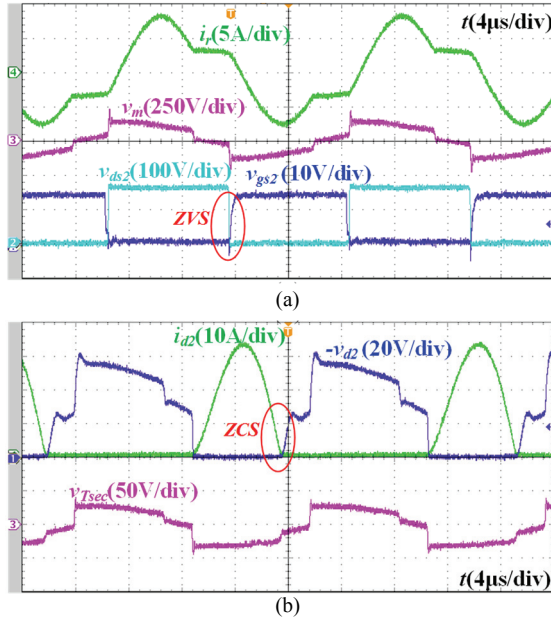
A laboratory prototype is built to verify the performance of the proposed converter. The main parameters of the prototype

TABLE I  
 KEY PARAMETERS OF THE CONVERTER

Component	Parameter
$L_r$	20 $\mu$ H
$C_r$	150nF
$L_m$	120 $\mu$ H
$S_1$ and $S_2$	Infineon's IPP50R199CP
$D_1$ and $D_2$	ST's STPS41L60CT
$n$	13:3
Magamp core	VAC W481
$n_{sr}$	11ts
LLC Controller	TI's UCC25600



Fig. 9. Size comparison between a magamp and a MOSFET.


 Fig. 10. Switching waveforms in the VF mode: (a)  $i_r$ ,  $v_m$ ,  $v_{gs2}$  and  $v_{ds2}$ ; (b)  $i_{d2}$ ,  $v_{d2}$  and  $v_{Tsec}$ .

are shown as follows:  $V_{in}=160\text{--}300\text{V}$ ,  $V_o=25\text{V}$ , output power  $P_o=400\text{W}$  and  $f_0=92\text{kHz}$ . The key components of the prototype are shown in Table I. The diameter of the magamp core is 15.5 mm and the height is 5.7 mm. A size comparison between a magamp and a MOSFET with a TO-220 package is shown in Fig. 9.

Fig. 10(a) and Fig. 10(b) show steady state experimental waveforms of the LLC-MAP converter in the VF mode with  $V_{in}=160\text{V}$  and  $I_o=16\text{A}$ . As shown in these waveforms,  $S_1$  and

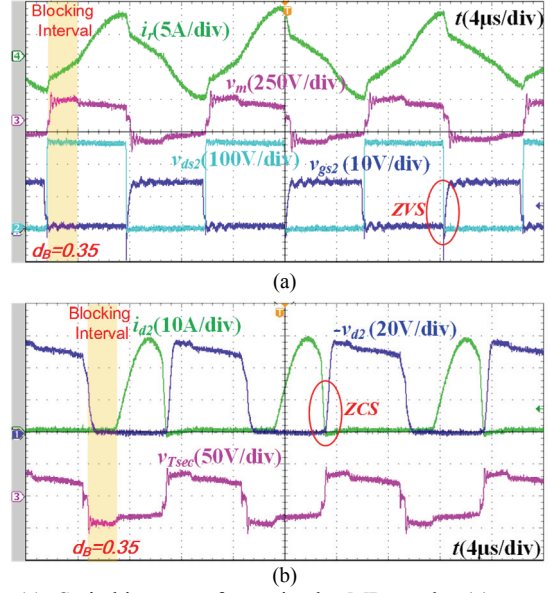
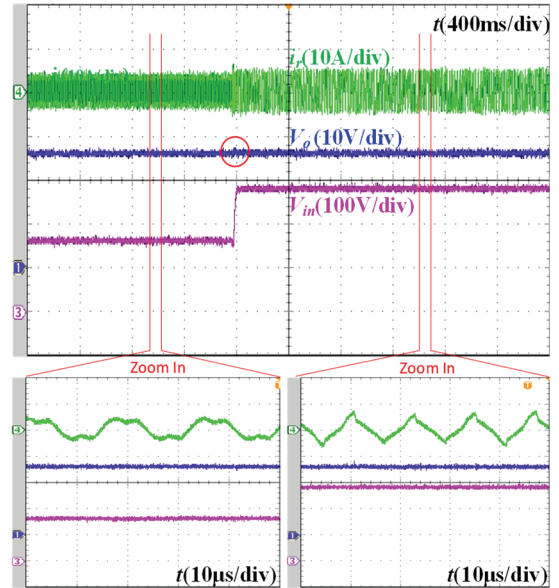

 Fig. 11. Switching waveforms in the MR mode: (a)  $i_r$ ,  $v_m$ ,  $v_{gs2}$  and  $v_{ds2}$ ; (b)  $i_{d2}$ ,  $v_{d2}$  and  $v_{Tsec}$ .


Fig. 12. Experimental waveforms of mode transitions.

$S_2$  operate under the ZVS condition and the full ZCS of  $D_1$  and  $D_2$  have been achieved.

Fig. 11(a) and Fig. 11(b) show steady state experimental waveforms in the MR mode with  $V_{in}=300\text{V}$  and  $I_o=15\text{A}$ . As can be seen, the blocking ratio  $d_B$  is 0.35.  $S_1$  and  $S_2$  operate under the ZVS condition. Since the slope of the current flowing through  $D_2$  in the MR mode is greater than that in the VF mode,  $D_2$  has a slight reverse recovery current. However, due to the current limiting effect of the primary side resonant inductor  $L_r$ , the reverse recovery of  $D_2$  is negligibly small. It is still considered that  $D_1$  and  $D_2$  satisfy the ZCS condition. These waveforms are well matched with the analysis.

Dynamic waveforms with input-voltage steps from 160V



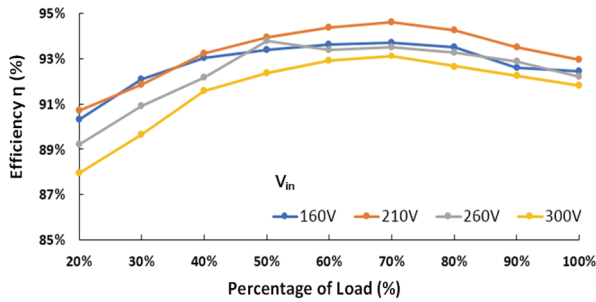


Fig. 13. Measured efficiency with different values of  $V_{in}$ .

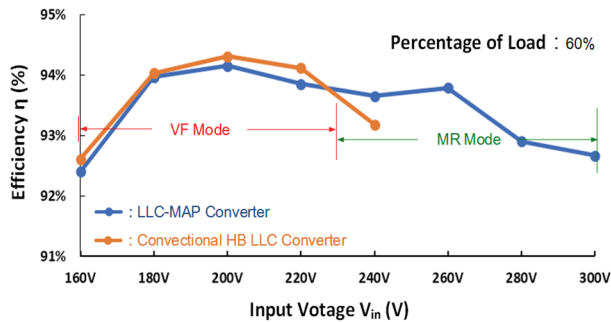


Fig. 14. Efficiency Comparison.

up to 280V are shown in Fig. 12. The overshoot of the output, which is about 2% of the output regulation, is extremely small. This indicates a good performance between the mode transition periods since the magamp loop and the LLC loop share the same controller.

Efficiency curves tested under different loads are shown in Fig. 13. When the input voltage varies from 160V to 300V, the highest efficiency is up to 94.6%. The best efficiency curve is obtained when  $V_{in}=210\text{V}$  since both the switching losses and conduction losses achieve an optimal balance. When the input voltage is 160V, the inverter operates in the VF mode within the full load range. Correspondingly, when the input voltage is 300V, the LLC-MAP converter operates in the MR mode within the full range. Moreover, since the conduction loss associated with the circulation current and the loss of the magamp increase when a wide input-voltage range is covered by the MR mode, the curve at 300V is below the one at 210V. However, in practical applications, the converter usually operates at half load or 3/4 load. Even if the input voltage is 300V, the efficiency of the converter is still above 92%.

Fig. 14. shows an efficiency comparison between the LLC-MAP converter and the conventional HB LLC converter at a 60% load with the same key parameters. The LLC-MAP converter setting  $f_{max}$  is 100 kHz. Since the maximum frequency of the utilized controller chip is 350 kHz, the upper limit of the operating frequency of the conventional HB LLC converter is about 340 kHz. The measured efficiency of the conventional HB LLC converter is approximately 0.3% higher than the LLC-MAP converter in the VF mode region.

This difference can be attributed to the copper loss of the magamp auxiliary post-regulator. At 240V, the efficiency of the conventional HB LLC converter is lower than that of the LLC-MAP converter due to the increasing of the switching loss since the converter operates at a very high frequency. A conventional HB LLC converter cannot regulate the output when the input-voltage is higher than 240V due to limitations on the switching frequency. However, the LLC-MAP converter switches to the MR mode as early as when the input voltage is 230V. In the MR mode region, since  $V_{in}$  increases,  $t_B$  increases accordingly. As a result, the increment of the core loss of the magamp leads to a reduction in efficiency. However, the overall efficiency is still high. To improve the efficiency, a synchronous rectifier can be used in the converter. It should be noted that this is a compromise between the conversion efficiency and the operational voltage range.

The input-voltage range of the proposed LLC-MAP converter is 1.75 times that of the conventional HB LLC converter. The proposed converter can be combined with the primary-side topology morphing solutions to further extend the operation ranges of the conventional LLC resonant converter.

## V. CONCLUSIONS

A very simple method for extending the input-voltage range of a HB LLC resonant converter has been proposed and verified in this paper. In comparison with the conventional HB LLC converter, magamp auxiliary post-regulators are added. Duty cycle control of the magamp post-regulator is applied to the converter when a dc gain smaller than unity is needed for the high input-voltage range. This method can narrow the switching-frequency range of a converter. ZVS have been achieved for the primary switches and ZCS has been realized for the secondary diodes. Experimental results from a laboratory prototype verify the effectiveness and feasibility of the proposed solution.

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