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# Three-coil Magnetically Coupled Resonant Wireless Power Transfer System with Adjustable-position Intermediate Coil for Stable Transmission Characteristics

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### Abstract

In magnetically coupled resonant (MCR) wireless power transfer (WPT) systems, the introduction of additional intermediate coils is an effective means of improving transmission characteristics, including output power and transmission efficiency, when the transmission distance is increased. However, the position of intermediate coils in practice influences system performance significantly. In this research, a three-coil MCR WPT system is adopted as an exemplification for determining how the spatial position of coils affects transmission characteristics. With use of the fundamental harmonic analysis method, an equivalent circuit model of the system is built to reveal the relationship between the output power, the transmission efficiency, and the spatial scales, including the axial, lateral, and angular misalignments of the intermediate and receiving coils. Three cases of transmission characteristics with deliberate adjustments in the position of the intermediate and receiving coils. A prototype of the three-coil MCR WPT system is built and analyzed, and the experimental results are consistent with those of the theoretical analysis.

Key words: Intermediate coil, Magnetically coupled resonant, Spatial scales, Stable transmission characteristics, Wireless power transfer

## I. INTRODUCTION

The concept of wireless power transfer (WPT) based on magnetic coupling theory was proposed by Nikola Tesla more than a century ago [1]. WPT uses magneto-quasistatic fields to transfer energy over short to medium distances and has been increasingly applied in electric vehicles, consumer electronics, and implantable medical devices due to its superiority and usability in humid and lousy environments [2]-[4]. Magnetically coupled resonant (MCR) WPT technology can deliver power efficiently over medium distances [5]. The basic MCR WPT system usually consists of two coils, namely, transmitting and receiving coils, which operate at the same resonant frequency. Numerous studies have focused on the analysis, design, and optimization of the basic two-coil MCR WPT system [6]-[8], whose output power and transmission efficiency noticeably drop with increased transfer distance [9] or the variation of position in space [10], [11].

For further enhancement of transmission characteristics, intermediate coils were introduced between the transmitting and receiving coils of the MCR WPT system in previous works. Three- and four-coil MCR WPT systems have been extensively proposed for increasing output power and transmission efficiency, particularly in long-distance applications [12], [13]. Similar to the position of coils in a two-coil WPT

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system, that in a three-coil WPT system considerably influences the transmission characteristics. Studies have been conducted to reveal the effect of intermediate coil on the performance of a system. [14] showed that three-coil inductive links can significantly improve transmission efficiency, particularly at long coupling distances, by transforming any arbitrary load impedance to the optimal impedance required at the input of the inductive link. The transmission efficiency of WPT with an intermediate coil was analyzed in [15], and the results showed that the intermediate resonant system had good transmission efficiency and was superior to nonintermediate systems. [16] discovered that placing an intermediate coil slightly near the transmission coil achieved better transmission efficiency than placing it slightly near the receiving coil. In [17], a three-coil WPT system structure was proposed and proven capable of significantly reducing the electromagnetic field emission caused by coil misalignment. In [18], the influence of spatial scales on the output power of three-coil system was investigated, but only one variable spatial scale was analyzed, meanwhile, the transmission efficiency was not considered.

In this paper, the transmission characteristics of a threecoil MCR WPT system versus the spatial scales, including axial, lateral, and angular misalignments, are discussed for stabilizing the output power and transmission efficiency at varying positions of the intermediate and receiving coils. Section II describes the basic theories and the key parameters of the three-coil MCR WPT system. According to equivalent circuit theory, the circuit model of the three-coil MCR WPT system is built, and the expressions of the output power and transmission efficiency are derived by the fundamental harmonic analysis (FHA) method. In Section III, the transmission characteristics of the system are analyzed and illustrated when the mutual inductances between the three coils are proportional. We find that the robustness of the output power and the transmission efficiency can be improved by an adjustment in the position of the intermediate coil according to the receiving coil. A prototype of the three-coil MCR WPT system is built and tested to validate the theoretical analysis in Section IV, which is followed by the conclusion in Section V.

# II. MODELING AND ANALYSIS OF TRANSMISSION CHARACTERISTICS

Fig. 1 shows the circuit diagram of the three-coil MCR WPT system, which includes a half-bridge inverter; a voltage doubler rectifier; and three resonant coils, namely, the transmitting, intermediate, and receiving coils. The mutual inductances between two adjacent coils are defined as  $M_{12}$  and  $M_{23}$ , and the mutual inductance between transmitting and receiving coils is ignored for simplification. The input voltage is inverted by the half-bridge inverter and employed to drive



Fig. 1. Configuration of the three-coil MCR WPT system.



Fig. 2. Equivalent circuit of the system.

the resonant coils.  $Q_1$  and  $Q_2$  are the power switches driven in a complementary manner with the same duty cycle.

Fig. 2 shows the equivalent circuit of the three-coil MCR WPT system, where  $U_s$  is the equivalent alternating voltage source,  $L_1-L_3$  are the self-inductances of the resonant coils, with parasitic resistances  $R_1-R_3$ .  $C_1-C_3$  are the series resonant capacitors designed to resonate with  $L_1-L_3$ .  $R_s$  is the impedance of the AC voltage source.  $R_W$  is the equivalent load resistance.

For the half-bridge configuration, the norm of  $\dot{U}_s$  can be calculated as

$$U_{s} = \left\| \dot{U}_{s} \right\| = \frac{\sqrt{2}}{\pi} V_{in}. \tag{1}$$

The equivalent load resistance  $(R_W)$  can be expressed by the load resistance  $(R_L)$  as

$$R_W = \frac{2}{\pi^2} R_L. \tag{2}$$

The resonant frequency is defined as

$$f_r = 1 / \left( 2\pi \sqrt{L_r \cdot C_r} \right), \tag{3}$$

where  $L_r$  and  $C_r$  are the resonant inductor and capacitor, respectively. If the three-coil MCR WPT system operates in a resonant state, then  $L_1 = L_2 = L_3 = L_r$ , and  $C_1 = C_2 = C_3 = C_r$ .

According to Fig. 2 and Kirchhoff's voltage law, the following can be obtained:

$$\begin{bmatrix} R_{s} + R_{1} & j\omega M_{12} & 0\\ j\omega M_{12} & Z_{2} & j\omega M_{23}\\ 0 & j\omega M_{23} & R_{3} + R_{W} \end{bmatrix} \begin{bmatrix} \dot{I}_{1}\\ \dot{I}_{2}\\ \dot{I}_{3} \end{bmatrix} = \begin{bmatrix} \dot{U}_{s}\\ 0\\ 0 \end{bmatrix}$$
(4)

where  $\omega = 2\pi f_r$ , and  $\dot{I}_1 - \dot{I}_3$  are the fundamental harmonics of the resonant currents.

If  $R_{1S} = R_1 + R_S$  and  $R_{3W} = R_3 + R_W$ , then  $\dot{I}_1 - \dot{I}_3$  can be solved from (4).



Fig. 3. 3D graphs of  $P_o$  and  $\eta$  versus  $M_{12}$  and  $M_{23}$ : (a)  $P_o$ ; (b)  $\eta$ .



Fig. 4. Transfer characteristics under different loads: (a)  $P_0$  ( $R_L = 2 \Omega$ ); (b)  $P_0$  ( $R_L = 50 \Omega$ ); (c)  $\eta$  ( $R_L = 2 \Omega$ ); (d)  $\eta$  ( $R_L = 50 \Omega$ ).

$$\begin{cases} \dot{I}_{1} = \frac{U_{S}(\omega^{2}M_{23}^{2} + R_{2}R_{3W})}{\omega^{2}M_{12}^{2}R_{3W} + \omega^{2}M_{23}^{2}R_{1S} + R_{1S}R_{2}R_{3W}} \\ \dot{I}_{2} = \frac{-jU_{S}\omega M_{12}R_{3W}}{\omega^{2}M_{12}^{2}R_{3W} + \omega^{2}M_{23}^{2}R_{1S} + R_{1S}R_{2}R_{3W}} \\ \dot{I}_{3} = \frac{-U_{S}\omega^{2}M_{12}M_{23}}{\omega^{2}M_{12}^{2}R_{3W} + \omega^{2}M_{23}^{2}R_{1S} + R_{1S}R_{2}R_{3W}} \end{cases}$$
(5)

Therefore, the output power of the system  $P_o$  can be expressed as

$$P_{o} = \frac{U_{s}^{2} \omega^{4} M_{12}^{2} M_{23}^{2} R_{W}}{\left(\omega^{2} M_{12}^{2} R_{3W} + \omega^{2} M_{23}^{2} R_{1s} + R_{1s} R_{2} R_{3W}\right)^{2}}$$
(6)

Radiation and power losses are ignored for simplification. Thus, the transmission efficiency  $\eta$  can be derived as

$$\eta = \frac{\omega^4 M_{12}^2 M_{23}^2 R_W}{(\omega^2 M_{23}^2 + R_2 R_{3W}) (\omega^2 M_{12}^2 R_{3W} + \omega^2 M_{23}^2 R_{15} + R_{15} R_2 R_{3W})}$$
(7)

From (6) and (7), the 3D graphs of the output power and the transmission efficiency versus  $M_{12}$  and  $M_{23}$  are illustrated in Fig. 3, and the specifications are as follows:  $V_{in} = 24 \text{ V}$ ,  $f_s =$  $f_r = 200 \text{ kHz}$ ,  $R_s = 0.1 \Omega$ ,  $R_L = 5 \Omega$ ,  $R_1 = 0.093 \Omega$ ,  $R_2 = 0.21 \Omega$ , and  $R_3 = 0.093 \Omega$ . The values of  $R_1$ – $R_3$  are measured by the impedance network analyzer and adjusted according to the experimental results. Fig. 3 indicates that  $P_o$  and  $\eta$  are sensitive to variations in  $M_{12}$  and  $M_{23}$  and  $P_o$  and  $\eta$  generally decrease with  $M_{12}$  and  $M_{23}$ .

In realistic applications,  $R_L$  always changes. Fig. 4 plots how  $R_L$  influences  $P_o$  and  $\eta$ , from which we can conclude that  $P_o$  decreases with an increase in  $R_L$  in a specific variation range of  $M_{12}$  (or  $M_{23}$ ). However, the variation of  $R_L$  has less influence on  $\eta$  compared with that of  $P_o$ . For simplification, the following analysis is based on a constant  $R_L$  (5  $\Omega$ ).

# III. ANALYSIS OF SPATIAL SCALES FOR STABLE OUTPUT POWER AND TRANSMISSION EFIFFIENCY

As transmission characteristics are subject to the variation of mutual inductances in a three-coil MCR WPT system, the possibility of achieving stable transmission characteristics by the adjustment of mutual inductances should be determined.

Fig. 5 shows the contour lines extracted from Fig. 3 by the insertion of horizontal planes into Fig. 3 with different magnitudes that represent diverse transfer characteristics, from which we can conclude that  $P_o$  and  $\eta$  can remain stable within specific ranges if  $M_{12}$  is proportional to  $M_{23}$ .

If  $M_{23} = k \cdot M_{12}$  and k is the proportional coefficient, then (6) can be simplified as

$$P_{o} = \frac{1}{\left(a_{1} + \frac{a_{2}}{M_{12}^{2}}\right)^{2}}$$
(8)

$$\begin{aligned}
\left\{a_{1} = \frac{R_{1S}}{U_{S}\sqrt{R_{W}}} \cdot k + \frac{R_{3W}}{U_{S}\sqrt{R_{W}}} \cdot \frac{1}{k} \\
a_{2} = \frac{R_{1S}R_{2}R_{3W}}{U_{S}\omega^{2}\sqrt{R_{W}}} \cdot \frac{1}{k}
\end{aligned}$$
(9)

and (7) can be simplified as

η

$$=\frac{1}{\frac{b_1b_3}{M_{12}^4}+\frac{b_1b_4+b_2b_3}{M_{12}^6}+\frac{b_2b_4}{M_{12}^8}}$$
(10)

$$\begin{cases} b_{1} = \frac{1}{\omega^{2} R_{W}} \\ b_{2} = \frac{R_{2} R_{3W}}{\omega^{4} R_{W}} \cdot \frac{1}{k^{2}} \\ b_{3} = \frac{R_{1s}}{\omega^{2} R_{W}} \cdot k^{2} + \frac{R_{3W}}{\omega^{2} R_{W}} \cdot \frac{1}{k^{2}} \\ b_{4} = \frac{R_{1s} R_{2} R_{3W}}{\omega^{4} R_{W}} \cdot \frac{1}{k^{2}} \end{cases}$$
(11)

where  $a_1$ ,  $a_2$ ,  $b_1$ ,  $b_2$ ,  $b_3$ , and  $b_4$  are constants related to the system parameters and k.

Based on (8)-(11) and  $M_{23} = k \cdot M_{12}$ , two clusters of curves of  $P_o$  and  $\eta$  versus  $M_{12}$  are illustrated in Fig. 6, which infers that coefficient k considerably influences  $P_o$  and  $\eta$ . If k is



Fig. 5. Contour with various mutual inductances: (a)  $P_o$ ; (b)  $\eta$ .



Fig. 6. Curves of  $P_o$  and  $\eta$  versus  $M_{12}$ : (a)  $P_o$ ; (b)  $\eta$ 



Fig. 7. 3D graphs of mutual inductance versus lateral and angular misalignments.

designed appropriately (for example,  $k \ge 1$ ), then  $P_o$  and  $\eta$  will be nearly stable within a specific range of  $M_{12}$ . Theoretically, k can be random in practice, as shown in Fig. 6. To simplify the analysis, we select k = 1.

To further investigate the requirements on spatial scales to achieve stable transmission characteristics, the relationships between mutual inductances and spatial scales are first obtained [19]. Fig. 7 illustrates the behavior of mutual inductance under lateral and angular misalignments and indicates that misalignments substantially affect mutual inductance. With the substitution of the mutual inductance into (8) and (10), the tendency of  $P_o$  and  $\eta$  versus the spatial scales can be determined.

#### Case 1: One variable spatial scale

In this study, three typical spatial scales are considered in the following analysis, namely, the axial misalignment (d), the



Fig. 8. Coil layout with axial, lateral, and angular misalignments.



Fig. 9. Curves of  $P_o$  and  $\eta$  versus  $d_{12}$ : (a)  $P_o$ ; (b)  $\eta$ .



Fig. 10. Curves of  $P_o$  and  $\eta$  versus  $\Delta_3$ : (a)  $P_o$ ; (b)  $\eta$ .

lateral misalignment ( $\Delta$ ), and the angular misalignment ( $\alpha$ ), as shown in Fig. 8. Meanwhile, three different cases are discussed, namely, one-, two-, and three-variable spatial scales. The specifications are given as follows:  $r_1 = r_2 = r_3 = 0.11$  m,  $N_1 = N_3 = 6$ , and  $N_2 = 14$ .

## 1) Axial Misalignment d ( $\Delta = 0, \alpha = 0$ )

With the assumption that  $d_{23} = k_d \cdot d_{12}$ , Fig. 9 shows the clusters of curves of  $P_o$  and  $\eta$  versus  $d_{12}$  under different  $k_d$  values. A remarkable discrepancy exists between the curves with different  $k_d$  values, and most curves fluctuate on a large scale. When  $k_d = 1$  ( $M_{23} = M_{12}$ ), the variation of  $P_o$  and  $\eta$  is relatively minor within the specific range of  $d_{12}$  ( $0 \le d_{12} \le 0.2$  m), which means that the transmission characteristics of the system are approximately constant. However, if  $k_d \ne 1$  or  $d_{12} > 0.2$  m, then  $P_o$  and  $\eta$  will fluctuate severely, which is detrimental to providing a stable power for loads.

#### 2) Lateral Misalignment $\Delta$ ( $d = 0, \alpha = 0$ )

With the assumption that  $\Delta_2 = k_{\Delta} \cdot \Delta_3$ , Fig. 10 illustrates how  $k_{\Delta}$  affects the tendency of  $P_o$  and  $\eta$  under different  $\Delta_3$  values. We can infer that  $P_o$  is more sensitive to  $k_{\Delta}$  than  $\eta$  to  $k_{\Delta}$ . Moreover, when  $k_{\Delta} = 0.5$  ( $M_{23} = M_{12}$ ),  $P_o$  and  $\eta$  decrease



Fig. 11. Curves of  $P_o$  and  $\eta$  versus  $\alpha_3$ : (a)  $P_o$ ; (b)  $\eta$ .



Fig. 12.  $P_o$  and  $\eta$  versus  $d_{12}$  and  $\Delta_3$ : (a)  $P_o$ ; (b)  $\eta$ .



Fig. 13.  $P_o$  and  $\eta$  versus  $\Delta_3$  and  $\alpha_3$ : (a)  $P_o$ ; (b)  $\eta$ .

slightly, which means that  $k_{\Delta}=0.5$  is also the best when only lateral misalignment is considered.

# 3) Angular Misalignment $\alpha$ ( $d = 0, \Delta = 0$ )

With the assumption that  $\alpha_2 = k_{\alpha} \cdot \alpha_3$ , Fig. 11 illustrates the correlation between  $P_o$ ,  $\eta$ , and  $\alpha_3$ , where the maximal  $\alpha_3$  is supposed to be 90°. Compared with other curves, the ones when  $k_{\alpha}$  equals 0.5 ( $M_{23} = M_{12}$ ) are nearly constant over the full range of  $\alpha_3$ , which means that if  $\alpha_2$  is strictly the half of  $\alpha_3$  ( $0 \le \alpha_3 \le 90^\circ$ ), then the system can always realize stable transmission characteristics.

From the above analysis, we can conclude that if only one spatial scale is considered, then a specific spatial range exists to keep the transmission characteristics of the three-coil MCR WPT system stable under the following conditions:  $d_{23} = d_{12}$ ,  $\Delta_2 = 0.5 \cdot \Delta_3$ , or  $\alpha_2 = 0.5 \cdot \alpha_3$ .

#### Case 2: Two-variable spatial scales

Under the constraints of  $d_{23} = d_{12}$ ,  $\Delta_2 = 0.5 \cdot \Delta_3$ , and  $\alpha_2 = 0.5 \cdot \alpha_3$ , the transmission characteristics of the three-coil MCR



Fig. 14.  $P_o$  and  $\eta$  versus  $\Delta_3$  and  $\alpha_3$ : (a)  $P_o$ ; (b)  $\eta$ .



Fig. 15.  $P_o$  and  $\eta$  with axial, lateral, and angular misalignments: (a)  $P_o$ ; (b)  $\eta$ .

WPT system when any two variable spatial scales are considered are analyzed as follows.

Figs. 12–14 demonstrate the curves of  $P_o$  and  $\eta$  versus  $d_{12}$ ,  $\Delta_3$ , and  $\alpha_3$ . As shown in Fig. 12,  $P_o$  and  $\eta$  decrease with the increase of  $d_{12}$  and  $\Delta_3$ . However, the transmission characteristics present less sensitivity to  $\alpha$  than to d and  $\Delta$ , as shown in Figs. 13 and 14. The spatial scale ranges for stable  $P_o$  and  $\eta$  are  $d_{12} \leq 0.2$  m,  $\Delta_3 \leq 0.25$  m, and  $\alpha_3 \leq 90^\circ$  under the given specifications, which are consistent with those of the one-variable spatial scale.

#### Case 3: Three-variable spatial scales

Fig. 15 shows the curve clusters of  $P_o$  and  $\eta$  versus three spatial scales under the conditions of  $d_{23} = d_{12}$ ,  $\Delta_2 = 0.5 \cdot \Delta_3$ , and  $\alpha_2=0.5 \cdot \alpha_3$ . The transmission characteristics decay with the increasing axial misalignment. In a specific range ( $d_{12} \le 0.1$  m), lateral and angular misalignments only slightly impact  $P_o$  and  $\eta$ ; thus, the curves (red) are noticeably near each other and change smoothly. However, when  $d_{12} > 0.1$  m,  $P_o$  and  $\eta$  are



Fig. 16. Photo of the prototype.

TABLE ISpecifications of the System

Parameters         Value         Parameters $V_{in}$ 24 V $L_1$ $R_S$ 0.1 $\Omega$ $L_2$ $f_s$ 200 kHz $L_3$ $r_1 \_ r_3$ 11 cm $C_1$	<b>Value</b> 16.7 µН
$V_{in}$ 24 V $L_1$ $R_S$ 0.1 $\Omega$ $L_2$ $f_s$ 200 kHz $L_3$ $r_1 \_ r_3$ 11 cm $C_1$	16.7 uH
$\begin{array}{ccc} R_S & 0.1 \ \Omega & L_2 \\ f_s & 200 \ \text{kHz} & L_3 \\ r_1 r_3 & 11 \ \text{cm} & C_1 \end{array}$	
$f_s$ 200 kHz $L_3$ $r_1 r_3$ 11 cm $C_1$	66.87 µH
$r_1 r_3$ 11 cm $C_1$	16.66 µH
	40.46 nF
$N_1$ 6 turns $C_2$	9.425 nF
$N_2$ 14 turns $C_3$	40.42 nF
$N_3$ 6 turns $R_L$	5 Ω

considerably influenced by lateral and angular misalignments, as shown by the blue and green curves. Meanwhile, axial and lateral misalignments have a greater influence on the transmission characteristics than does the angular misalignment.

From the analysis above, we can deduce that the three-coil MCR WPT system can realize a stable power transfer within a specific spatial scale range if the positions of the three coils are appropriately arranged to guarantee equal or proportional mutual inductances between two adjacent coils.

The misalignment range for stable  $P_0$  and  $\eta$  is not fixed because the transfer characteristics of the system depend on multiple parameters. Therefore, in practice, the misalignment range for stable  $P_0$  and  $\eta$  is determined by the specification of the system, especially by the proportional coefficient, *k*.

## IV. EXPERIMENTAL VERIFICATION

To validate the theoretical analysis, a prototype of the three-coil MCR WPT system is built in the laboratory, as shown in Fig. 16, and the specifications are listed in Table I.

Figs. 17–19 show the theoretical and experimental results of the output power and transmission efficiency versus the one-variable spatial scales, respectively, where the solid curves represent the theoretical results and the dashed ones are the experimental data.

Figs. 20-22 illustrate the curves of the output power and transmission efficiency versus the two-variable spatial scales,



Fig. 17. Theoretical and experimental data with different axial misalignments ( $d_{12} = d_{23}$ ,  $\Delta_2 = \Delta_3 = 0$  m,  $\alpha_2 = \alpha_3 = 0^\circ$ ): (a)  $P_o$ ; (b)  $\eta$ .



Fig. 18. Theoretical and experimental data with different lateral misalignments ( $d_{12} = d_{23} = 0.25$  m,  $\Delta_2 = 0.5 \Delta_3$ ,  $\alpha_2 = \alpha_3 = 0^\circ$ ): (a)  $P_{o}$ ; (b)  $\eta$ .



Fig. 19. Theoretical and experimental data with different angular misalignments ( $d_{12} = d_{23} = 0.25$  m,  $\Delta_2 = \Delta_3 = 0$  m,  $\alpha_2 = 0.5 \alpha_3$ ): (a)  $P_{o}$ ; (b)  $\eta$ .

respectively. The experimental results are also generally consistent with the theoretical results.

Fig. 23 demonstrates the output power and transmission efficiency at three spatial scales. As depicted, the angular misalignment has less effect on the transmission characteristics than do the axial and lateral misalignments; and this finding is consistent with the analysis in Section III.

Fig. 24 shows the key experimental waveforms under different spatial scales, where  $i_1$  and  $i_3$  are the currents of the transmitting and receiving coils, respectively. As shown in Fig. 24, the phase difference between  $i_1$  and  $i_3$  is 180°. Before the switch turns on, the drain current is negative, which indicates that the drain-to-source voltage ( $v_{ds}$ ) is clamped to zero and the switch can achieve zero-voltage-switching.



Fig. 20. Theoretical and experimental data with different axial and lateral misalignments ( $d_{12} = d_{23}$ ,  $\Delta_2 = 0.5 \Delta_3$ ,  $\alpha_2 = \alpha_3 = 0^\circ$ ): (a)  $P_o$  ( $\Delta_3 = 0$  m); (b)  $\eta$  ( $\Delta_3 = 0$  m); (c)  $P_o$  ( $\Delta_3 = 0.1$  m); (d)  $\eta$  ( $\Delta_3 = 0.1$  m).



Fig. 21. Theoretical and experimental value with variant lateral and angular misalignments ( $d_{12} = d_{23} = 0.25$  m,  $\Delta_2 = 0.5 \Delta_3$ ,  $\alpha_2 = 0.5 \alpha_3$ ): (a)  $P_o(\Delta_3 = 0$  m); (b)  $\eta(\Delta_3 = 0$  m); (c)  $P_o(\Delta_3 = 0.1$  m); (d)  $\eta(\Delta_3 = 0.1$  m).



Fig. 22. Theoretical and experimental value with variant axial and angular misalignments: (a)  $P_o(d_{12} = 0 \text{ m})$ ; (b)  $\eta(d_{12} = 0 \text{ m})$ ; (c)  $P_o(d_{12} = 0.22 \text{ m})$ ; (d)  $\eta(d_{12} = 0.22 \text{ m})$ .



Fig. 23. Theoretical and experimental data with different axial, lateral and angular misalignments: (a)  $P_o (d_{12}=0.1 \text{ m}, \alpha_3=0^\circ)$ ; (b)  $\eta (d_{12}=0.1 \text{ m}, \alpha_3=0^\circ)$ ; (c)  $P_o (d_{12}=0.1 \text{ m}, \alpha_3=90^\circ)$ ; (d)  $\eta (d_{12}=0.1 \text{ m}, \alpha_3=90^\circ)$ ; (e)  $P_o (d_{12}=0.25 \text{ m}, \alpha_3=0^\circ)$ ; (f)  $\eta (d_{12}=0.25 \text{ m}, \alpha_3=0^\circ)$ ; (g)  $P_o (d_{12}=0.25 \text{ m}, \alpha_3=90^\circ)$ ; (h)  $\eta (d_{12}=0.25 \text{ m}, \alpha_3=90^\circ)$ .



Fig. 24. Experimental waveforms: (a) Lateral misalignment ( $\Delta_2 = 0.5\Delta_3 = 5$  cm,  $\alpha_2 = \alpha_3 = 0^\circ$ ); (b) Angular misalignment ( $\Delta_2 = \Delta_3 = 0$  cm,  $\alpha_2 = 0.5\alpha_3 = 10^\circ$ ); (c) General misalignment ( $\Delta_2 = 0.5\Delta_3 = 5$  cm,  $\alpha_2 = 0.5\alpha_3 = 10^\circ$ ).

# V. CONCLUSIONS

This research investigates a three-coil MCR WPT system with transmitting, intermediate, and receiving coils. Via the equivalent circuit and FHA method, the output power and the transmission efficiency of the system with axial, lateral, and angular misalignments are analyzed in detail. We find that different spatial scales have varied influences on the transmission characteristics. Compared with axial and lateral misalignments, the angular misalignment has a minor impact on the system. By adjusting the position of the intermediate and receiving coils to ensure equal or proportional mutual inductances between two adjacent coils, the WPT system can achieve relatively stable transmission characteristics within a specific range of spatial scales. The conclusions are validated by experiments, whose results are consistent with those in the theoretical analysis.

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